晩期型恒星とその活動 ~晩期型恒星の彩層・コロナ~ ^{国立天文台} 渡邊鉄哉

●恒星の磁気活動

- 彩層:水素の電離と熱的分化
 - K(CaII)線 (non-LTE line formation)
 - ウィルソン・バップ効果と彩層の尺度則
- 遷移層のエネルギー収支 輻射損失と熱伝導
- ●コロナループの尺度則
 - diagnostics via CR-model
- 自転速度と活動性
- ●恒星の磁場・黒点
- 活動周期

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Chromospheric Activity measured by MgII h+k lines



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Correlation: Chromosphere vs

corona

Ayres et al., 1981, ApJ, 247, 545.









Energy Flux out of Stars

$$\nabla(\vec{F}_{r} + \vec{F}_{c} + \vec{F}_{m} + \vec{F}_{g} + \vec{F}_{k} + \vec{F}_{e}) = 0$$

$$\vec{F}_{r}; \text{ radiative } \vec{F}_{c}; \text{ conductive } \vec{F}_{m}; \text{ mechanical}$$

$$\vec{F}_{g}; \text{ gravitatio nal } \vec{F}_{k}; \text{ kinematic } \vec{F}_{e}; \text{ enthalpy}$$

at
$$\tau_{c} \sim 10^{-4}$$
 (T_{min}), $\Delta T \sim 150$ K
 $\Delta H/H \sim 16T^{3}/T_{eff}^{4} \Delta T \tau_{c} \sim 1.5 \times 10^{-5}$

Chromosphere; (3–6) $\times 10^{6}$ erg/cm²sec

 $\rightarrow \Delta H/H \sim (5-8) \times 10^{-5} \text{ erg/cm}^2 \text{sec}$

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水素の電離 electron donner at T_{min} ~metal at T_{top}~hydrogen

$$4\pi \frac{dH}{dz} = QA_{el}N_eN_Hf(\tau)g(\tau)$$

Q: collision strength A_{el} : element abundance $f(\tau) \sim \exp(-X_u/kT)$ collisional excitation $g(\tau) \sim \exp(\pm A/kT)$ lower level population

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hydrogen

$$L = \frac{dH}{dz}; \text{ energy loss rate /cm}^{3} \qquad \stackrel{n=2}{\xrightarrow{X_{2} \quad L_{\alpha}}}$$

$$\frac{d \ln T}{dz} = \frac{kT}{X_{u} \pm A} \left(\frac{d \ln L}{dz} - 2 \frac{d \ln N_{H}}{dz} \right) \quad N_{p} \ll \overline{N_{e}}$$

$$= \frac{kT}{X_{2} + (1 + \alpha)(X_{u} \pm A)} \times \qquad N_{p} \sim N_{e}$$

$$\left[(1 + \alpha) \frac{d \ln L}{dz} - (2 + \alpha) \frac{d \ln N_{H}}{dz} - \frac{d \ln(1 - \gamma)}{dz} \right]$$

$$\gamma = N_{p} / (N_{p} + N_{HI}) \quad X_{2}: n = 2 \text{ excitation energy}$$

$$\alpha = 1 \ (\tau_{LC} \gg 1) \xrightarrow{R_{e}} 0 \ (\tau_{LC} < 1)$$

$$N_{HI} \sim n_{p} n_{e}^{\alpha} \cdot e^{\frac{X_{2}}{kT}}$$



(i) Ne \leftarrow metal (ii) Ne \sim Np $\gamma <<1$ (iii) Ne \sim Np $\gamma \sim 1$

- . $X_u \pm A \ll X_2 \rightarrow (ii) dln T/dz \sim minimum$
- . $\gamma \sim 1$ temperature gradient max

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Empirical Chromospheric Model



A: dark point within a cell B: average cell center C: average quiet sun D average network E: bright network F: very bright network element F': flare (Fontenla et al. 1990)....



Thermal Bifurcation (Ayres 1981, ApJ 224, 1064.) coolant CO & heater/coolant H⁻ $F=e_{co}+e_{H}-$ (=0; radiative equilibrium) 4900K H⁻ cooling 5×10^{6} erg/cm²sec 4000 H⁺ heating 4000K CO dissociate Т 2900K 2900 4900

Two-level atom without continuum

radiative transfer

$$\mu \frac{dI_{v}}{dz} = \left[-n_{l}B_{lu}I_{v} + n_{u}(A_{ul} + B_{ul}I_{v}) \right] \phi_{v} \frac{hv}{4\pi}$$
$$S_{v} = \frac{n_{u}A_{ul}}{n_{u}B_{ul} - n_{l}B_{lu}} = \frac{2hv^{3}}{c^{2}} \left[\left(\frac{n_{l}g_{u}}{n_{u}g_{l}} \right) - 1 \right]^{-1}$$

statistical equilibrium

$$n_{l}\left(B_{lu}\int\phi_{v}J_{v}dv+C_{lu}\right)=n_{u}\left(A_{ul}+B_{ul}\int\phi_{v}J_{v}dv+C_{ul}\right)$$



Two level atom w/o cont.





等温でも吸収線ができる!



mean free path; I_{ν}

photon destruction probability; P_d

thermalization depth; Λ

photon escape probability; P_e

$$l_{v} \sim \frac{1}{\chi_{v}} = \frac{1}{\chi_{lu}\phi_{v} + \chi_{c}}$$
$$P_{d} \sim \frac{C_{ul}}{C_{ul} + A_{ul}}$$
$$\Lambda; \quad P_{e}(\tau) = P_{d}(\tau)$$
$$P_{e}(\tau) = \int_{x_{1}}^{\infty} \phi(x) dx$$
for $x_{1}; \tau_{x} = 1$

line profile $\phi(\mathbf{x}) \rightarrow$ thermalization depth Λ

Doppler;
$$\phi(x) = \frac{1}{\pi} e^{-x^2}$$

 $A \sim \frac{1}{\varepsilon}$
Voigt; $\phi(x) = \frac{a}{\pi\sqrt{\pi}} \int_{-\infty}^{\infty} e^{-y^2} [(x-y)^2 + a^2]^{-1} dy$
 $A \sim \frac{a}{\varepsilon^2}$
Lorentz; $\phi(x) = \frac{1}{\pi} \frac{1}{x^2 + 1}$
 $A \sim \frac{1}{\varepsilon^2}$

source function at the surface

$$S_l(0) = \sqrt{\varepsilon}B$$



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Wilson-Bappu Effect; Interpretation

- Chromospheric Thickness
- W₀; Dopper control?
- Inside K1, k1; optically thick in chromosphere
- ← effect of radiative transfer
- Ayres 1979, ApJ 228, 509

$$\frac{dF}{dm} \sim \frac{F^{tot}}{m_*}, \quad \text{*:temperature min.}$$

$$F^{tot} \sim F_{MgII}, \quad F_{MgII} / \sigma T_{eff}^4 \sim T_{eff}^{2\pm 2}$$

$$F_{\odot}^{tot} \sim 7 \times 10^6 \, erg \, / \, cm^2 s$$

$$\sim 7 \times 10^6 \, \tilde{F} \, T_{eff}^{6\pm 2}$$

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$$\frac{dF}{dm}_{*} \sim \frac{dF}{dm}_{H^{-}} \sim Cn_{e}^{*} \sim \frac{P^{*}}{T_{*}}\tilde{A}_{Fe}$$

$$T_{*} \sim 0.75T_{eff} \qquad P = mg \quad (hydrostatic)$$
_{経験的}

$$\tilde{A}_{Fe} \quad F \quad g \quad T_{eff}$$

Lorentzian wing control of K1

$$\begin{split} \tau_{\Delta\lambda_{*}} \sim \kappa_{l} \stackrel{\sim}{A}_{el} m_{*} \Delta \lambda_{*}^{-2} \\ \Delta\lambda_{*} \sim \kappa_{l}^{1/2} \left(\frac{\tilde{A}_{el}}{\tilde{A}_{Fe}} \right)^{-1/2} \tilde{A}_{Fe} \stackrel{1/4}{F} \tilde{g}^{-1/4} T_{eff}^{\frac{7}{4} \pm \frac{1}{2}} \\ \Delta\lambda_{*}^{k1} / \Delta\lambda^{kK1} \sim 2.5 \quad (\mathfrak{A}) \approx 2.3) \end{split}$$

TABLE

Adopted Line Parameters*

Са п К	Мg п k
3934	2796
21.5×10^{8}	2.7×10^{8}
0.70	0.63
1.5×10^{-6} 2 × 10^{-6}	3×10^{-5}
1.6 3.6×10^{6}	9.8 3.4 × 10 ⁷
5.8×10^{-7}	7.3×10^{-7}
	Ca II K 3934 2 1.5×10^8 0.70 1.5×10^8 2×10^{-6} 1.6 3.6×10^6 5.8×10^{-7} 1.9×10^{-15}

* From Shine 1973, Appendix A, unless otherwise indicated. † $f = 1.5 \times 10^{-16} \lambda A^2 (g_2/g_1) A_{21}$ (Allen 1973, p. 59). ‡ $\kappa_l \equiv (\pi e^2/m_e c) f(\lambda_l^4/c^2) (\Gamma_R/4\pi^2) (A_{el}^{\circ}/1.4m_{\rm H}).$ § $\kappa_{lc} \equiv (\pi e^2/m_e c) f(\lambda_l/\sqrt{\pi}) (A_{el}^{\circ}/1.4m_{\rm H}).$ || $\epsilon_l \equiv \Omega_{21}/A_{21} = [(g_1/g_2)\Omega_{12}/A_{21}].$

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 $\Lambda \sim \frac{1}{-}$ (thermalization length) $\tau_{I_c} \approx \kappa_{I_c} A_{el} \xi^{-1} m_{\Lambda} = \Lambda \sim (\varepsilon_I n_I)^{-1}$ $\mathcal{E}_{I} \equiv \Omega_{II} / A_{II}$ ξ : Doppler velocity ~ ~ 6 ± 2 ~ -1/2 ~ 1/2 ~ 1/2 ~ $5/2\pm 1$ $n_1 \sim F T_{eff} \quad m_*^{-1} \sim A_{Fe} \quad F \quad g \quad T_{eff}$ $n_l \sim \frac{dF}{dm} \sim \frac{F^{tot}}{m_{m}}$ chromosphere mean density $m_{\Lambda} \sim \kappa_{lc}^{-1} \varepsilon_{l}^{-1} \left(\frac{\tilde{A}_{el}}{\tilde{A}_{r}}\right)^{-1} \tilde{A}_{Fe}^{2/3} \tilde{F}^{-1/2} g^{-1/2} T_{eff}^{-(\frac{5}{2}\pm 1)} \xi$

 $\Delta \lambda_{\Lambda}^{k} / \Delta \lambda_{\Lambda}^{K} \sim 0.9$ (観測:太陽 ~1)



- W(K1), W(K2) ともg^{-1/4}でスケールする
- W(K2)~ ξ^{1/2} でスケールする
- W(K2) \uparrow F \downarrow , while W(K1) \uparrow F \uparrow

←観測 Osolar plage



遷移層・コロナ



遷移層のエネルギー収支ー輻射損失と熱伝導

(corona) $H_c = R_c + C_c$ (transition region) $H_{tr} + C_c = R_{tr}$

Observation: $R_{tr} \sim C_c \rightarrow H_{tr} \sim 0$



CR Modelling under coronal condition

• Line intensity of a permitted line $(j \rightarrow i)$ $j - \frac{h}{2} \sqrt{\frac{h}{\nu}} \sqrt{\frac{h}{\nu}}$ (Emissivity /volume) $i - \frac{h}{\nu}$ $N_{j} = \frac{N_{j}(X^{+m})}{N(X^{+m})} \frac{N(X^{+m})}{N(X)} \frac{N(X^{+m})}{N(Y)} \frac{N(X)}{N(H)} \frac{N(H)}{N_{i}} N_{e}$ $A_{ji} N_{j} = N_{e} C_{ij} N_{i} (X^{+m})$ (-radiative-collisional model $\varepsilon(\lambda_{ij}) = \frac{hc}{\lambda_{ij}} C_{ij} N_e N (X^{+m}) \text{ excited state } << \text{ground state}$ $C_{ij} = 8.63 \times 10^{-6} T_{e}^{-\frac{1}{2}} \frac{\Omega_{ij}}{\omega} \pi a_{0}^{2} \exp(-\frac{\Delta E_{ij}}{kT})$





G(T); contribution function



$$I = \beta \iiint G(T) N_e^2 dV$$

= $\beta G(T_m) \iiint N_e^2 dV$ (isothermal)
 $dV = dSdh \quad \frac{dT}{dh} \equiv \nabla T$
= $\beta \iiint G(T) N_e^2 \frac{1}{\nabla T} dSdT$

← differential emission measure



Classical transition region DEM analysis



図 5-32 XUVデータから求めた遷移域における温度と温度勾配との関係 点線 はデータをよく再現する線で、10⁵~10⁶Kの範囲では 熱伝導フラックスが一定 (T_e^{5/2}dT_e/dh=一定)なことを示す. Siの存在量を3×10⁻⁵とすると、(a)、(b)に 対する F_eの値はそれぞれ、3×10⁵ erg/cm² sec および 1×10⁶ erg/cm² sec となる (Athay, 1971). (a); 2電子再結合を含まない (Athay, 1966bによる). (b);電子 再結合を含む (Dupree & Goldberg, 1967による).

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コロナループの尺度則 $\frac{dF_c}{ds} = n_e^2 \chi T^{-\frac{1}{2}} - H, \quad H \sim const. (erg \cdot cm^{-3})$ $\chi \sim 10^{-18.81} (Raymond)$ $F_c dF_c \sim \left(\frac{p}{2k}\right)^2 \chi \kappa_0 dT - H \kappa_0 T^{\frac{5}{2}} dT, \quad F_c = \kappa_0 T^{\frac{5}{2}} \frac{dT}{ds}$ $\left(\frac{F_c}{2}\right)^2 \sim \left(\frac{p}{2k}\right)^2 \chi \kappa_0 (T - T_m) - \frac{7}{2} H \kappa_0 (T^{\frac{7}{2}} - T_m^{\frac{7}{2}})$ $T \sim 0$, $F_c \sim 0$ (thermally isolated) $\rightarrow H \sim \frac{7}{2} \left(\frac{p}{2k}\right)^2 \chi T_m^{-\frac{3}{2}}$

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Rosner, Tucker, & Viana (1978) Kano & Tsuneta (1995)

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Chromospheric Activity measured by MgII h+k lines



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S-index, R_{HK}, R'_{HK}

- Vaughan, Preston, Wilson (1978) $-S \sim H/(H_V+H_R) + K/(K_V+K_R)$
- Middelkoop (1982) : color correction $-R_{HK} \sim F_{HK}/(\sigma T_{eff}^4)$
- Noyes et al. (1984): photospheric contr. $-R'_{HK} = R_{HK} - R_{photo}$

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Figure 4 The K-line bandpass of the instrument used to produce the Vaughan-Preston (1980) survey and other Mount Wilson Ca II HK flux measurements, superimposed on both quiet Sun and plage spectra (Hartmann et al. 1984b).





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- Light-curve inversion
 - $-I_i = f_i I_s + (1 f_i)I_p f_i$: filling factor $0 \le f_i \le 1$
- Doppler imaging (Goncharskii et al. 77...)



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1000

500

T(phot)

Н



second order polynomial fit to the data excluding EK Dra. Dots in circles indicate solar umbra (T = 1700 K) and penumbra (T = 750 K).



Stellar Magnetic Fields – obs tech-

Robinson Jr., R. R. (1980)

Zeeman triplet: $\Delta \lambda (\Lambda) \propto 4.7 \times 10^{13} g \lambda^2 B (G)$ (g: = (g) = (g) (g) (g)

 $\mathsf{F}_{\lambda} = (1-f) \mathsf{F}_{\lambda} (\mathsf{B}{=}0) + f \mathsf{F}_{\lambda} (\mathsf{B}{\neq}0)$

5

4

2

0

0

20

3 F 🔘

Stellar Magnetic Field Measurements



Magnetic field measurements for active dwarfs (circles) and giants (squares) versus the photosphere temperature. Big circles indicate the sunspot umbra (B = 3 kG) and penumbra (B = 1.5 kG). The thick solid line is a linear fit to the data, excluding the sunspot umbra.

Magnetic field measurements for active dwarfs (circles) and giants (squares) versus the filling factor. Big circles indicate the sunspot umbra (B = 3 kG) and penumbra (B = 1.5 kG). The thick solid line is a linear fit to the data, excluding the sunspot umbra

40

Filling factor, %

60

80



T photosphere, K Filling factors of spots (open symbols) and magnetic fields (filled symbols) on the surfaces of active dwarfs (circles) and giants (squares) versus the photosphere temperature. The thick solid line is a polynomial fit to the spot filling factors. The dashed line is a fit to the magnetic field filling factor, excluding the Sun. A big circle emphasises the sunspot umbra (f ~1%). (Berdyugina, 2005, Living Rev. Solar Phys., 2, 8.) 55





Chromospheric Ca II emission cycles for Sun-like stars, illustrating the regular cyclic variation that is common in such stars. The Ca II emission is plotted in Mount Wilson "S-Index" units. From Radick (2000).

~100 Stars in spectral types of G0 - K5 V

- Young rapidly rotating stars
 - high average levels of activity
 - non-smooth cyclic variation.
- Stars of intermediate age (approximately 1 2 Gyr for 1M)
 - moderate levels of activity
 - occasional smooth cycles.
- Stars as old as the Sun and older
 - slower rotation rates
 - lower activity levels and smooth cycles.
- Stars of no variations
 - in the stage similar to the Maunder minimum
 - subgiants evolved off the main-sequence (Wright, 2004).
- vs. H/K chromospheric variation
 - young stars: anticorrelates with their variation in chromospheric emission \rightarrow activity cycles on young stars should be more prominent in spot patterns rather than in chromospheric plages.



Spot cycles in the solar irradiance and V magnitudes of the RS CVn binary σ Gem and two young solar analogues AB Dor and LQ Hya. Note that the maximum of the spot area corresponds to the maximum irradiance on the Sun and minimum brightness on the stars.

- Sun: maximum spot area at the maximum irradiance
- Active stars: maximum spot area at minimum brightness → periodic changes of spot rotation periods in phase with the spot cycle